

# Sortledton: a universal, transactional graph data structure

Submitted for VLDB 2022:

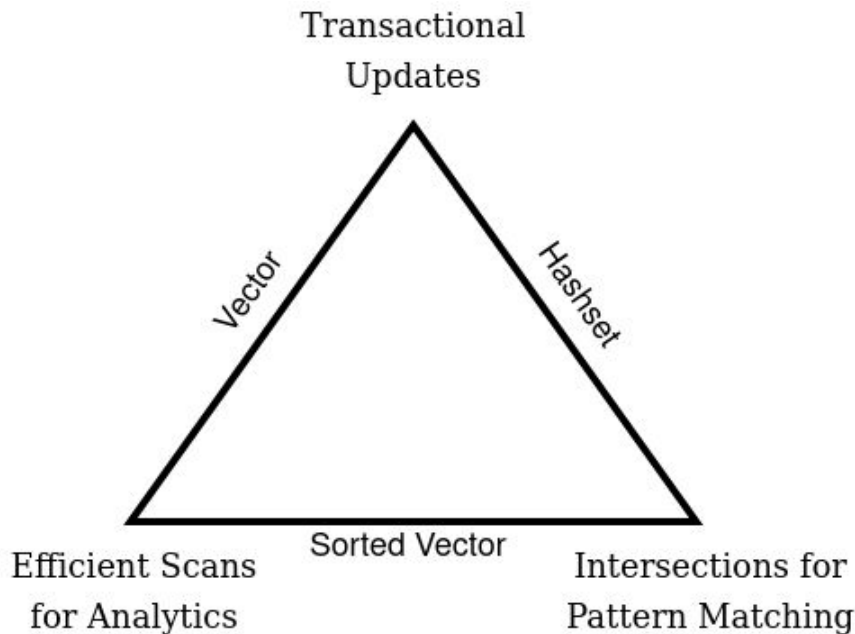
Per Fuchs, Domagoj Margan and  
Jana Giceva



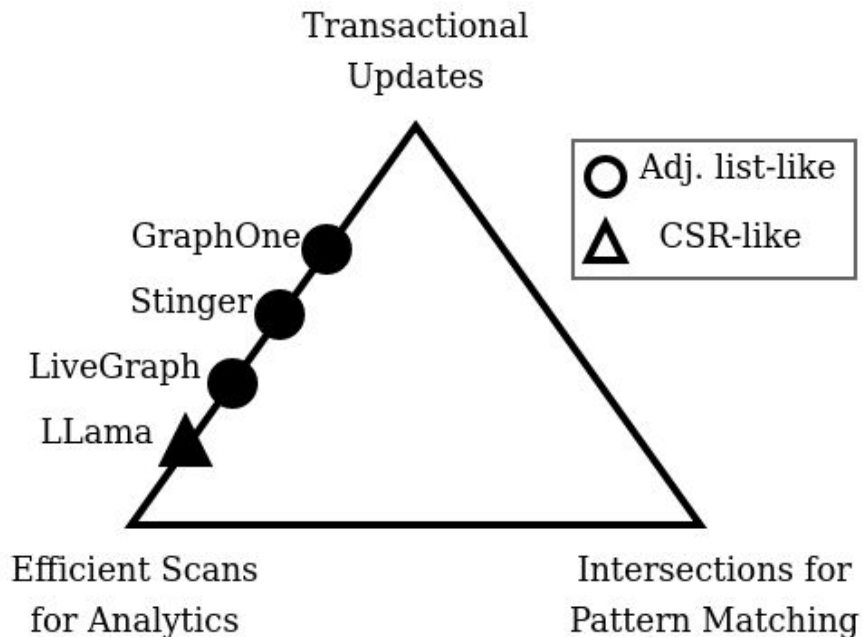
# Graph use-cases are diverse and dynamic

- *diverse*: use multiple graph workload categories, e.g. analytics, traversals and graph pattern matching (GPM)
- *dynamic*: requires insertions and deletions
  
- Examples:
  - Alibaba: analytics and traversals in anti-fraud-pipelines [VLDB'20]
  - Twitter: use of traversals and GPM for recommendations [VLDB'14, '15]
  - Both require up to 2 million edge insertions per second

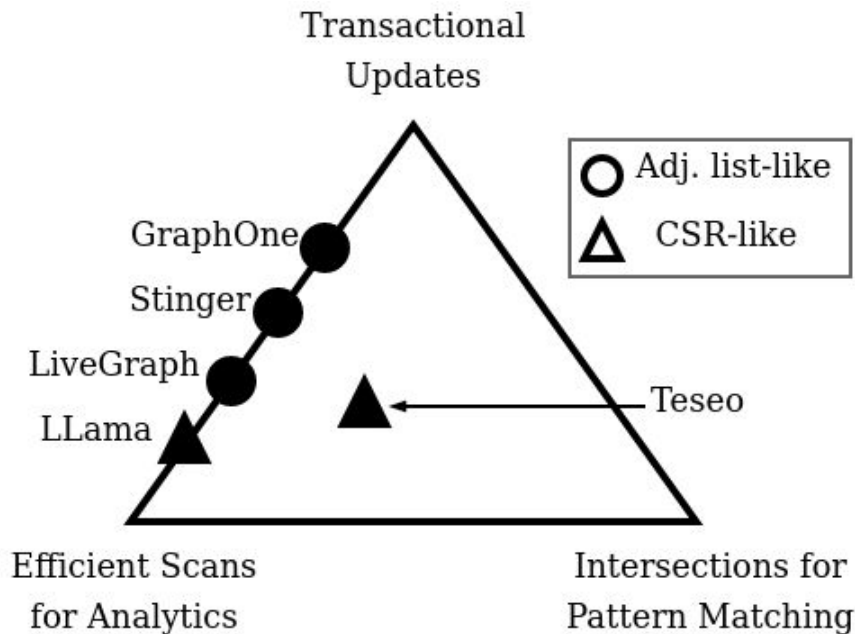
# New challenges in graph data structures: striking a good trade-off for all workloads



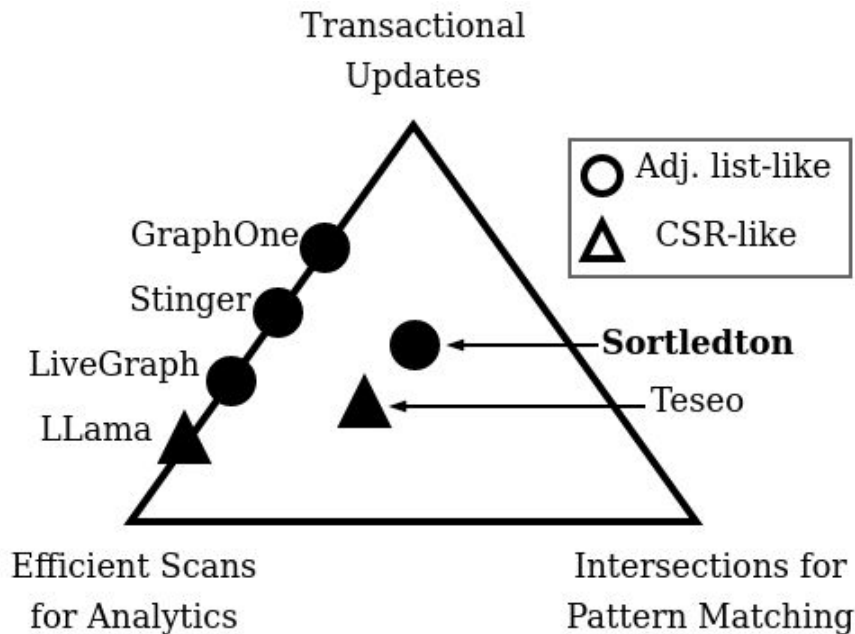
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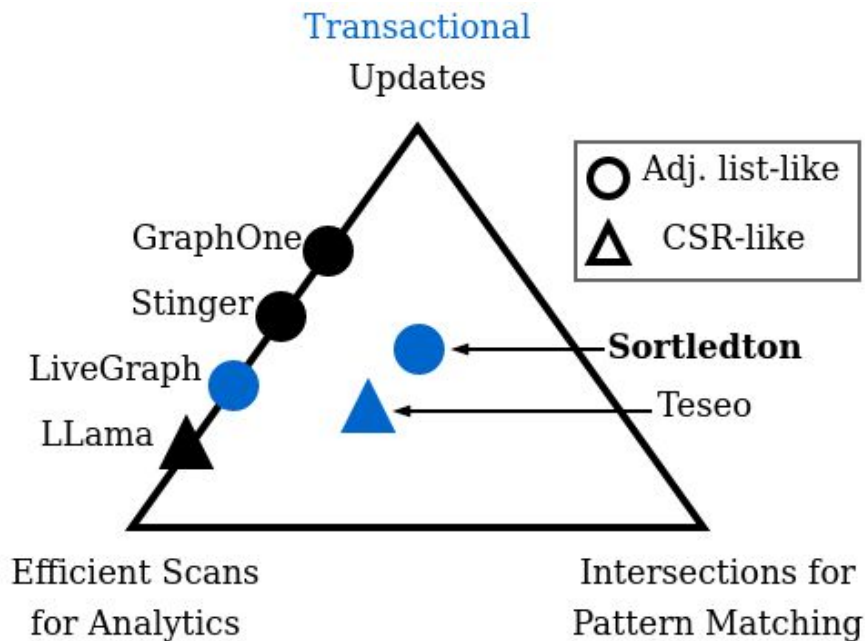
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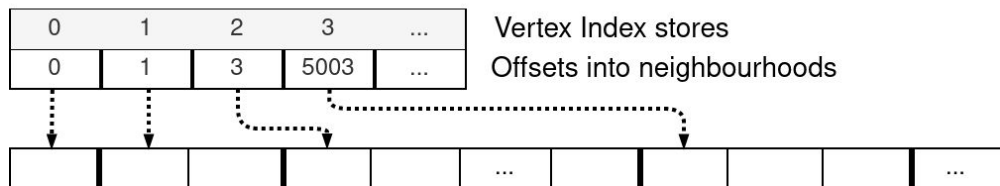
# Contributions

1. Comparison of fundamental graph data structure designs
2. Analysis of access patterns in graph workloads
3. A simple dynamic data structure design with memory consumption (2x CSR) and analytical performance (1.2x CSR)
  
4. Design of a graph specialized, serializable MVCC system (in the paper)



# Comparison of fundamental graph data structures

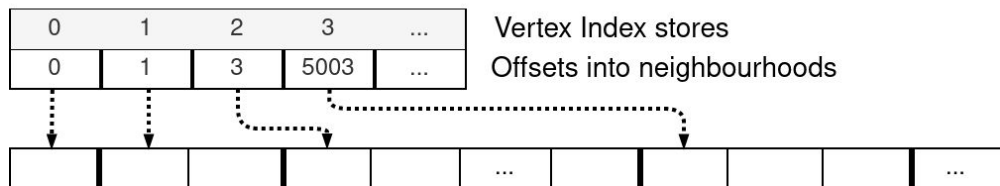
CSR-like



+ sequential vertex access

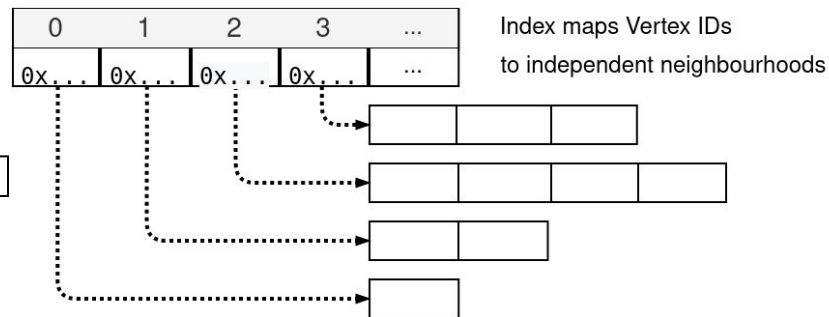
# Comparison of fundamental graph data structures

CSR-like



- + sequential vertex access

Adjacency List-Like



- + independent neighbourhoods
- + cheap index maintenance
- + reuse of existing data structures

# Graph access patterns

## Inner PageRank loop

```
1 for  $v \in V$  do  
2   | incoming  $\leftarrow 0$   
3   | for  $e \in v.\text{neighbours}$  do  
4   |   | incoming  $\leftarrow$  incoming + contrib[ $e$ ]  
5   | scores[ $v$ ]  $\leftarrow$  incoming
```

# Graph access patterns

## Inner PageRank loop

### 1. Sequential Vertex Access

```
1 for  $v \in V$  do  
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# Graph access patterns

## Inner PageRank loop

### 1. Sequential Vertex Access

```
1 for  $v \in V$  do
```

```
2   | incoming  $\leftarrow$  0
```

### 2. Sequential Neighbourhood Access

```
3   | for  $e \in v.\text{neighbours}$  do
```

```
4     | | incoming  $\leftarrow$  incoming + contrib[ $e$ ]
```

```
5   | | scores[ $v$ ]  $\leftarrow$  incoming
```

# Graph access patterns

## Inner PageRank loop

1. Sequential Vertex Access

2. Sequential Neighbourhood Access

3. Random Algorithmic-Specific Access

```
1 for  $v \in V$  do  
2   incoming  $\leftarrow 0$   
3   for  $e \in v.\text{neighbours}$  do  
4     | incoming  $\leftarrow$  incoming + contrib[ $e$ ]  
5   scores[ $v$ ]  $\leftarrow$  incoming
```

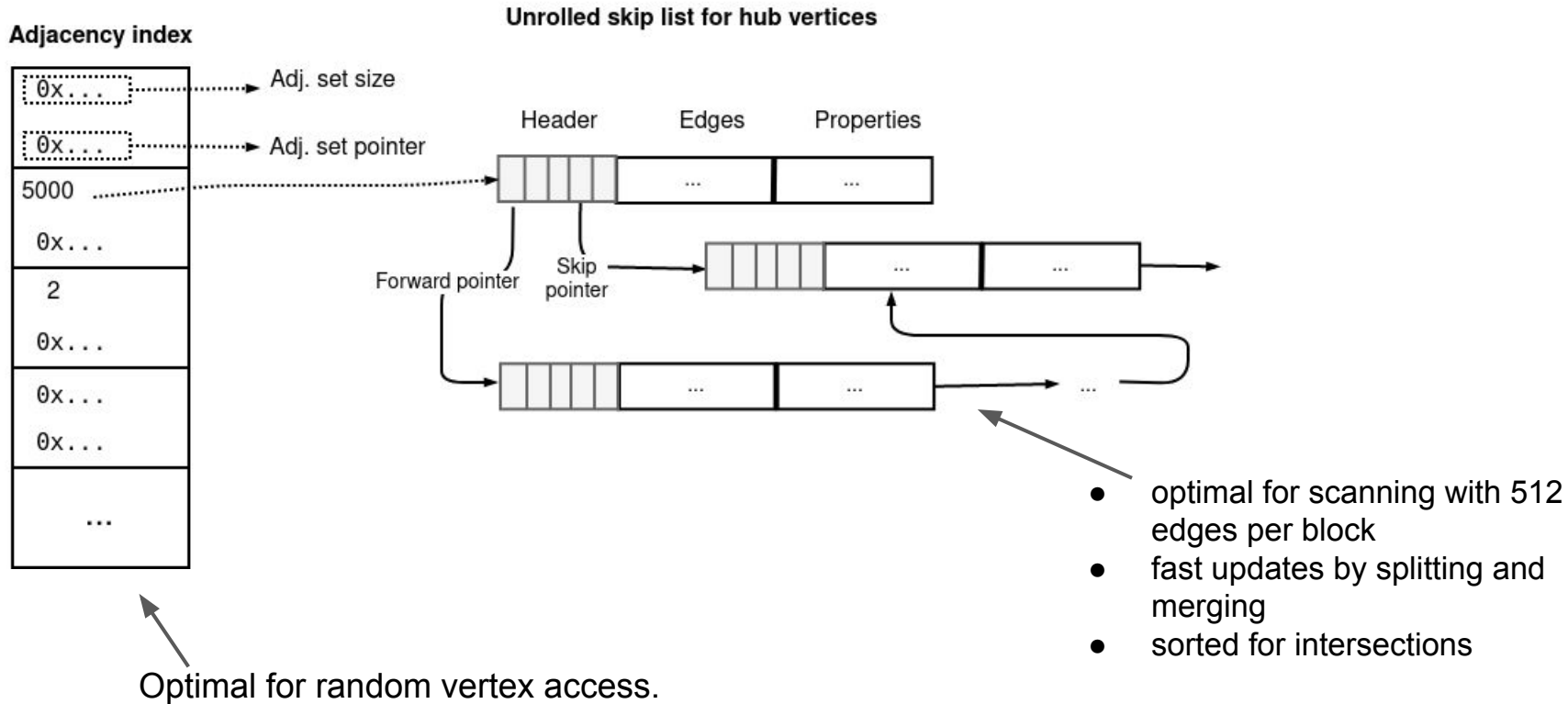
# Graph access patterns

## Inner PageRank loop

1. Sequential Vertex Access	1	<b>for</b> $v \in V$ <b>do</b>
	2	incoming $\leftarrow 0$
2. Sequential Neighbourhood Access	3	<b>for</b> $e \in v.\text{neighbours}$ <b>do</b>
3. Random Algorithmic-Specific Access	4	incoming $\leftarrow$ incoming + contrib[ $e$ ]
	5	scores[ $v$ ] $\leftarrow$ incoming

Optimizing for 2 and 3 has higher impact because mostly  $|E| / |V| > 30$ .

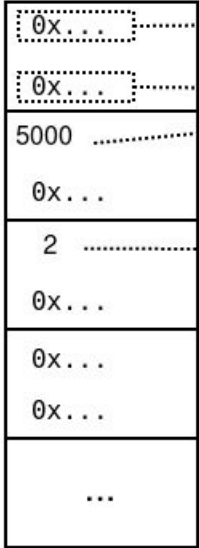
# Sortledton: simple and sorted





# Sortledton: simple and sorted

## Adjacency index

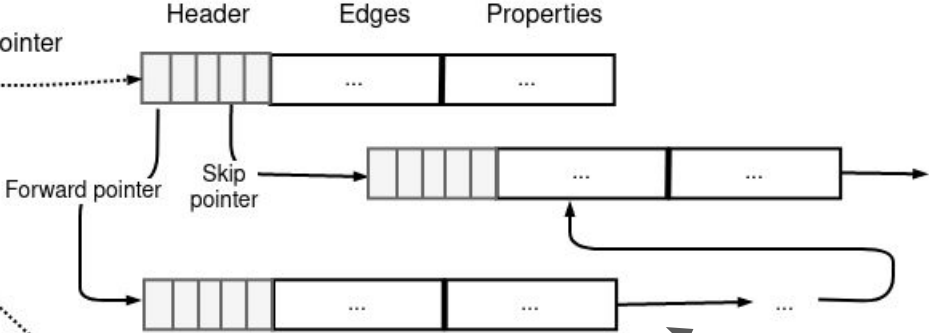


Adj. set size

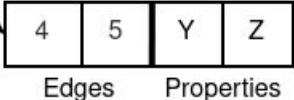
Adj. set pointer

Optimal for random vertex access.

## Unrolled skip list for hub vertices



## Vectors for small neighbourhoods

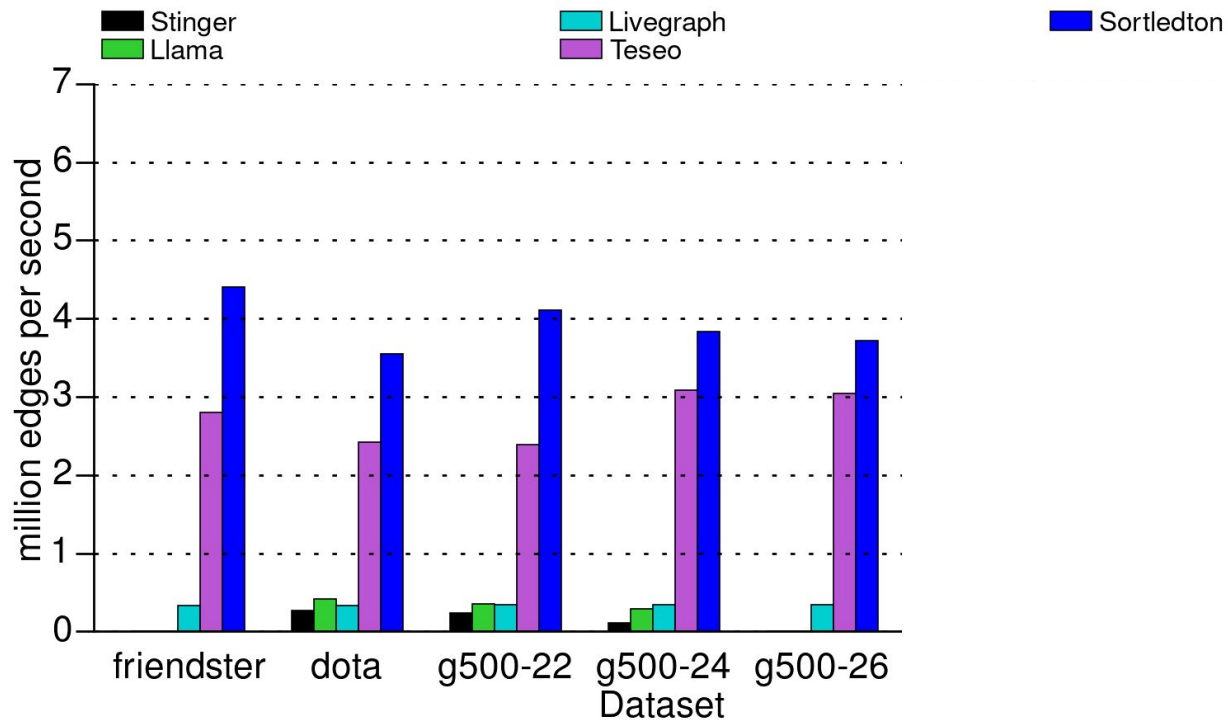


- optimal for scanning with 512 edges per block
- fast updates by splitting and merging
- sorted for intersections

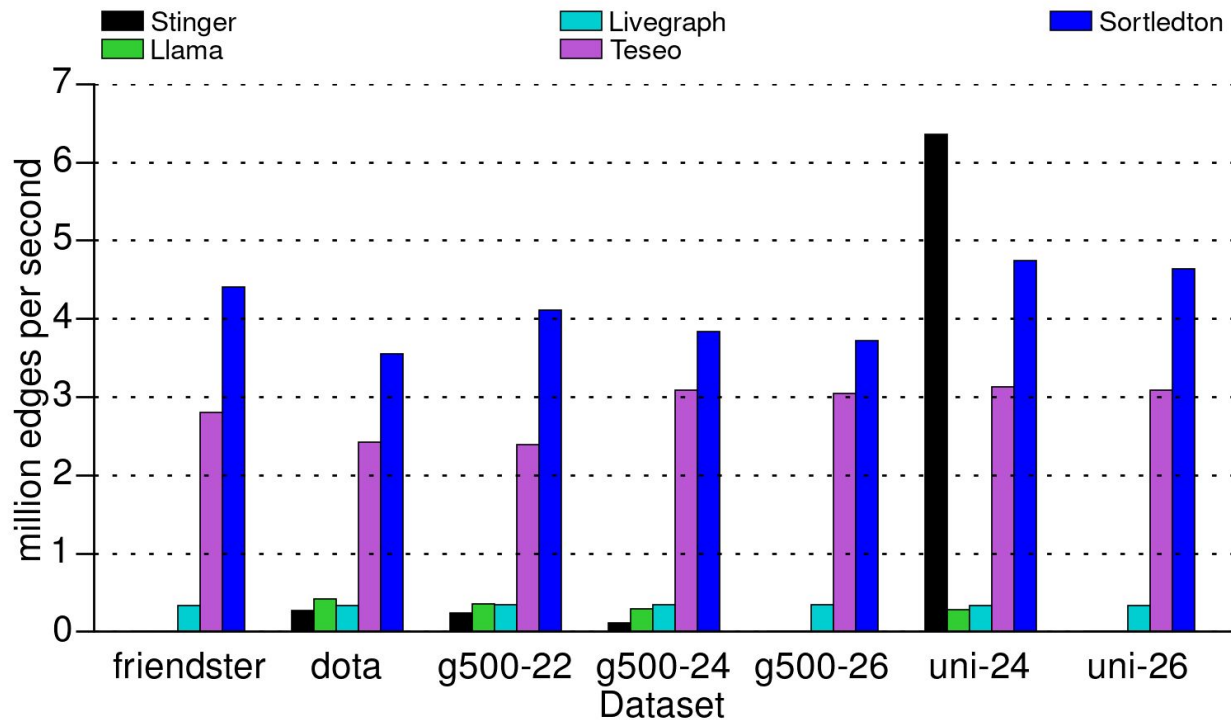
# Evaluation

- Update performance: how many updates can the data structures process?
  - Challenge is to find the existing edges
- Graphalytics Benchmark: what is the slowdown for different workload categories compared to a CSR?
- Not in the presentation:
  - Mixing updates and deletions to expose aging effects
  - Memory consumption over aging

# Update performance - power law graphs



# Update performance - uniform graphs

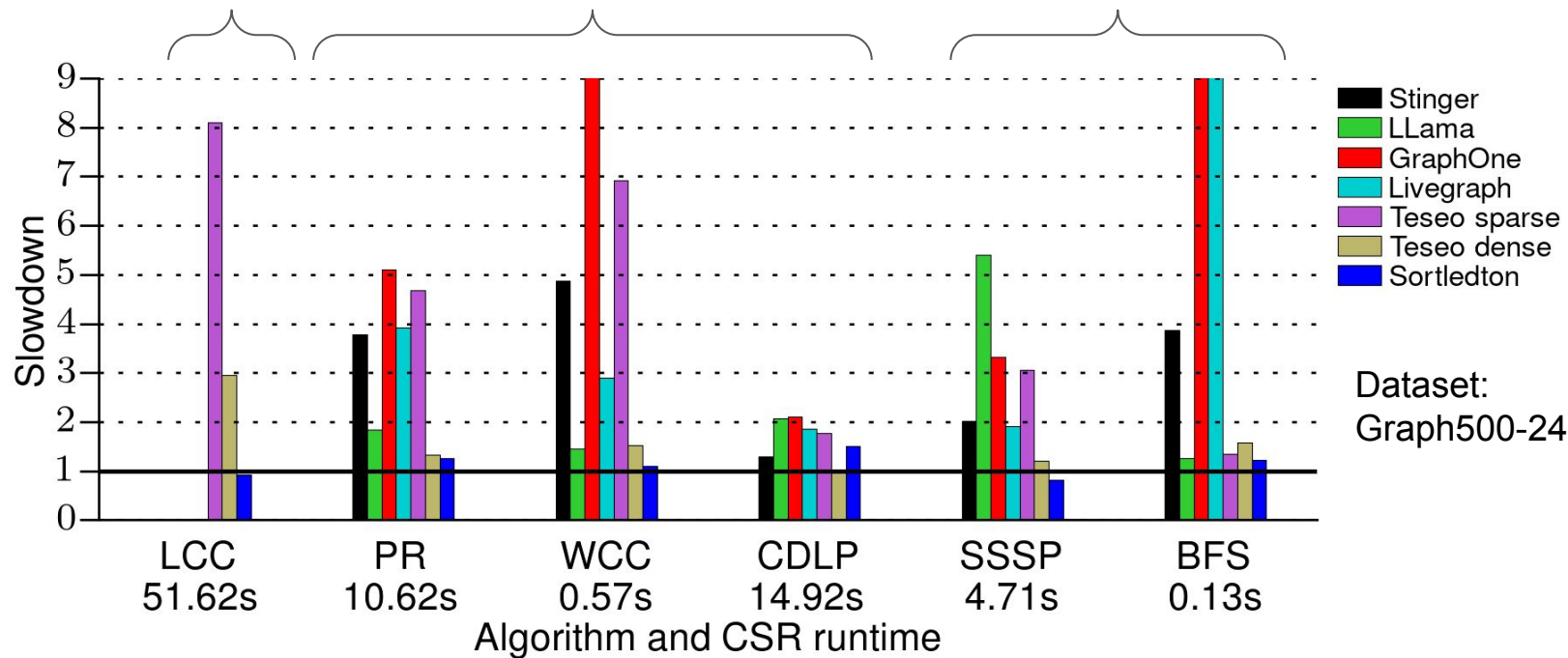


# Graphalytics benchmark performance

Graph Pattern Matching

Graph Analytics

Graph Traversals

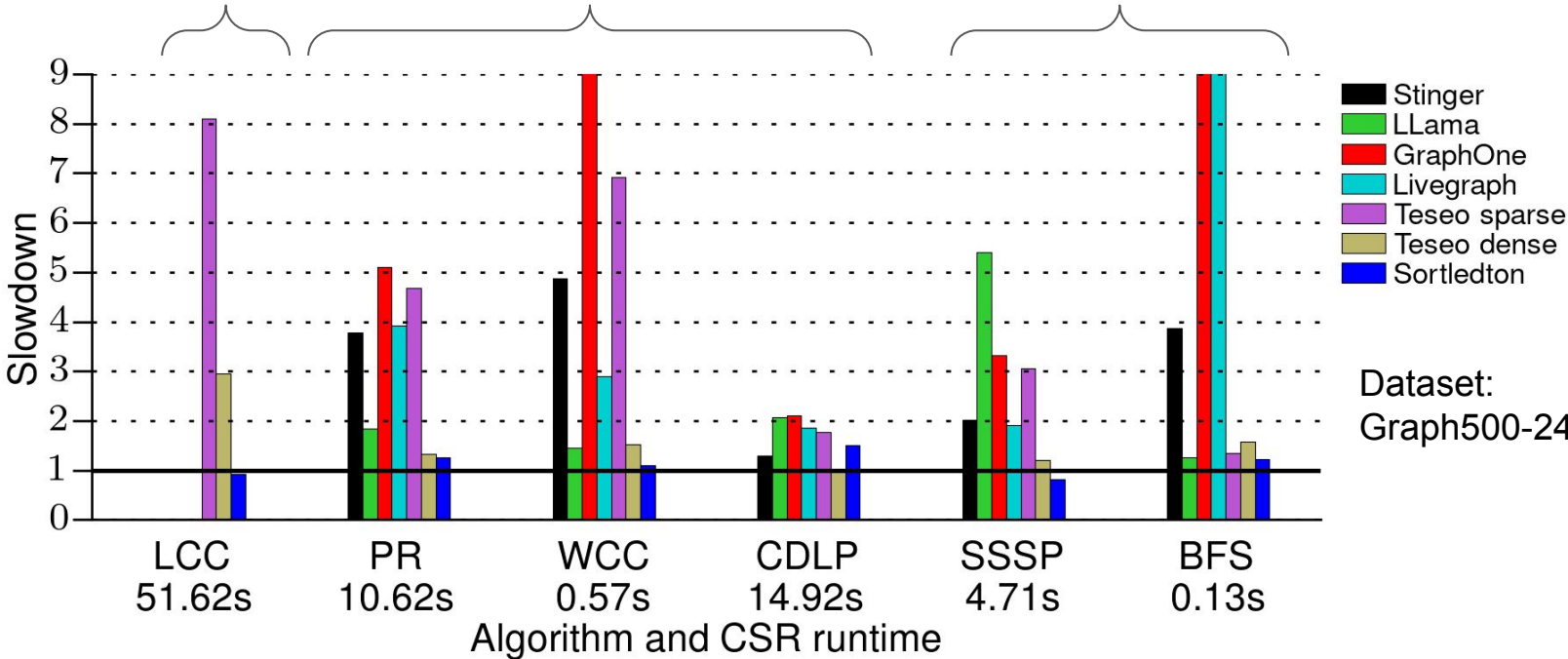


# Graphalytics benchmark performance

Graph Pattern Matching

Graph Analytics

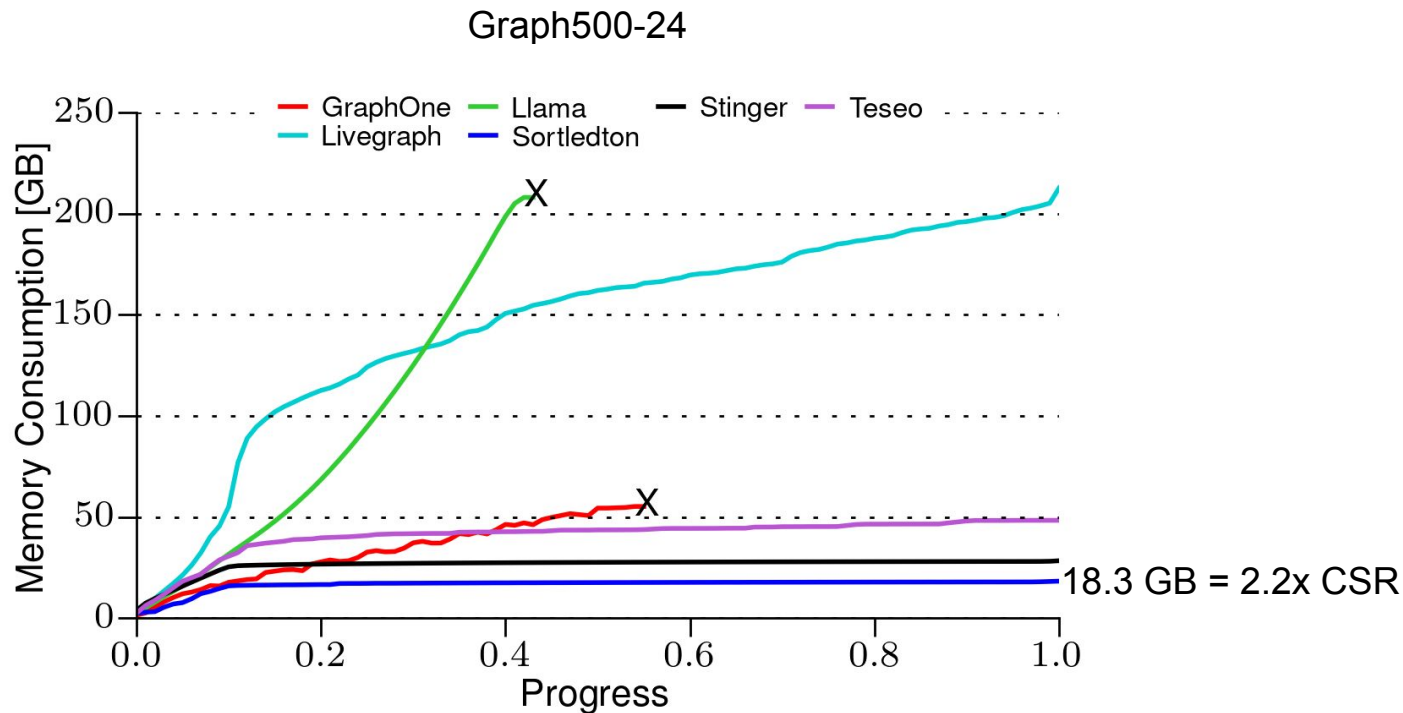
Graph Traversals



# Conclusions

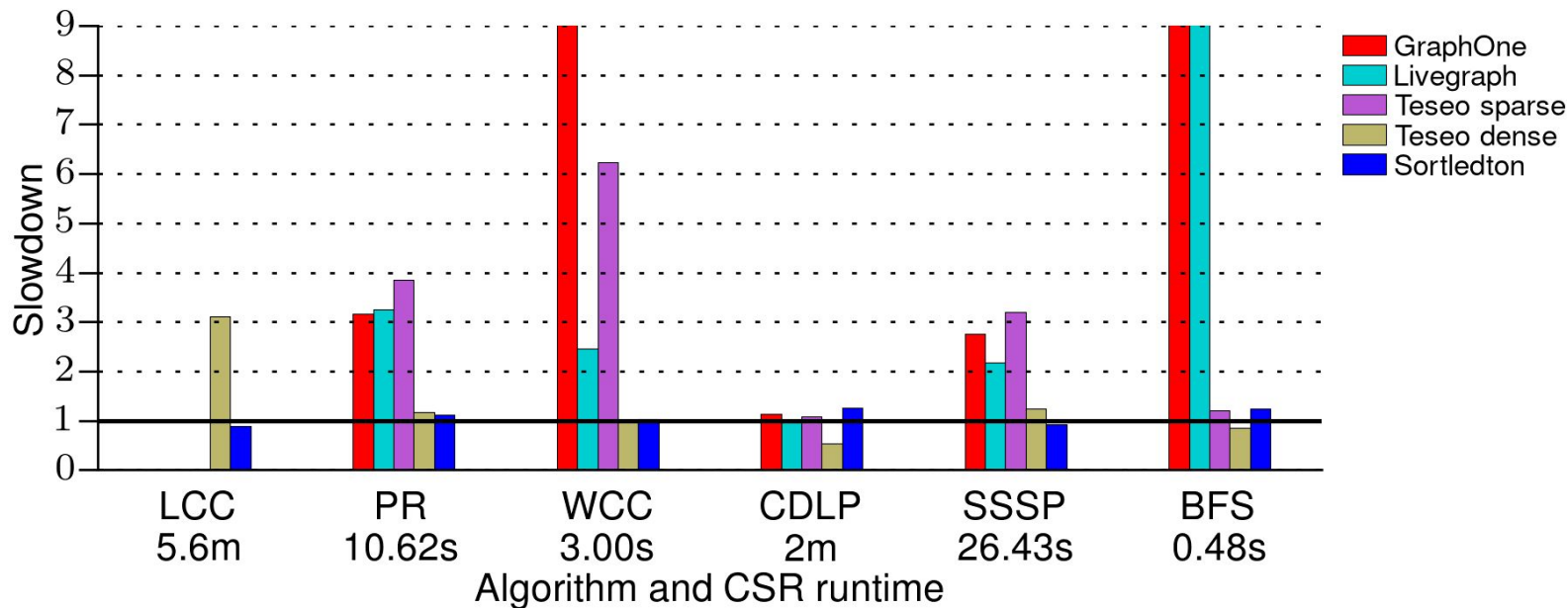
- adjacency list-like designs are simpler than CSR-like designs while showing equal performance
- we need to store neighbourhoods as sets to support GPM, updates, deletions and consistency

# Memory Footprint



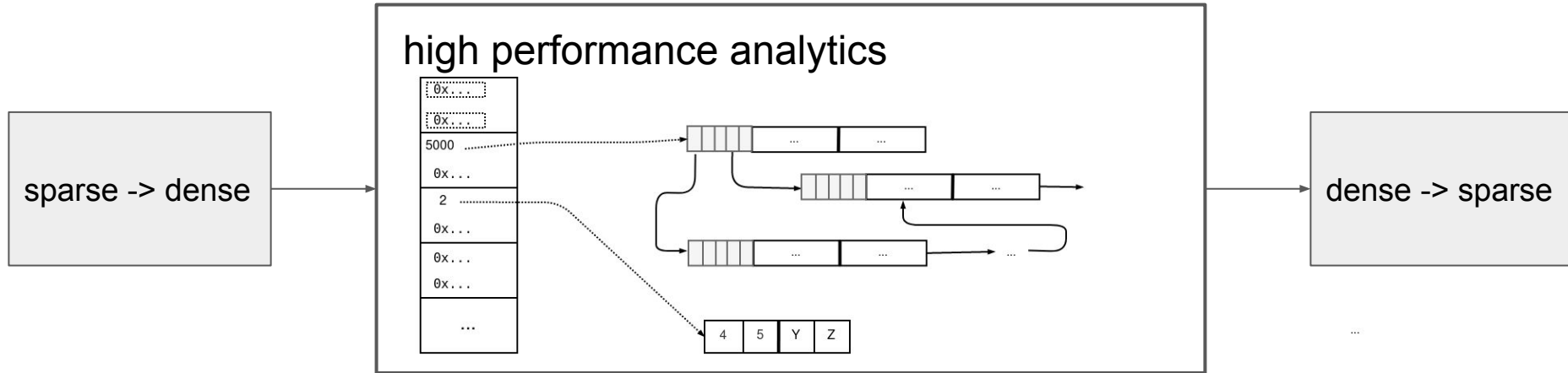


# Graphalytics Benchmark Performance



# Dense vertex identifier for algorithmic specific access

- we translate arbitrary vertex identifier {0, 5, 1000, ...} on insertion into the dense domain [0, 1, 2, ...] for better analytical performance



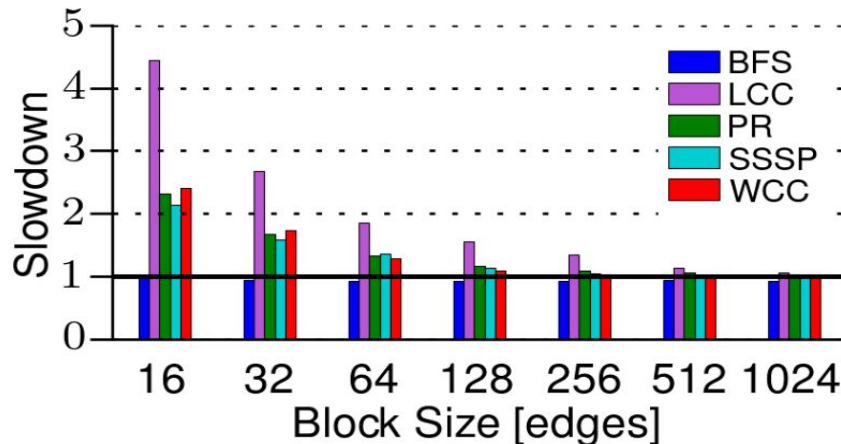
# Sorted Blocks for Sequential Edge Access with intersections

Sorted blocks for neighbourhoods

normalized against

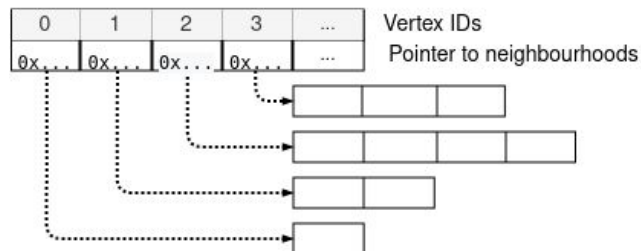
Sorted Vector for neighbourhoods (optimal, static)

Graphalytics Algorithms



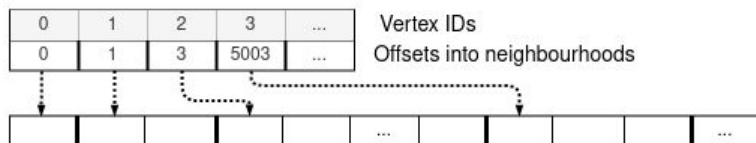
# Optimizing for Sequential Vertex Access

## Vector-based Adjacency List

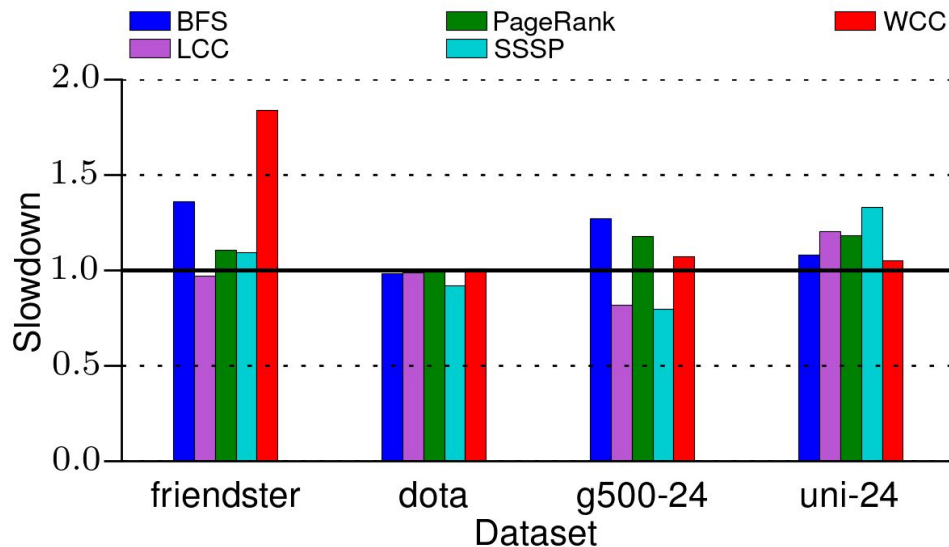


normalized against

## CSR



## Graphalytics Algorithms



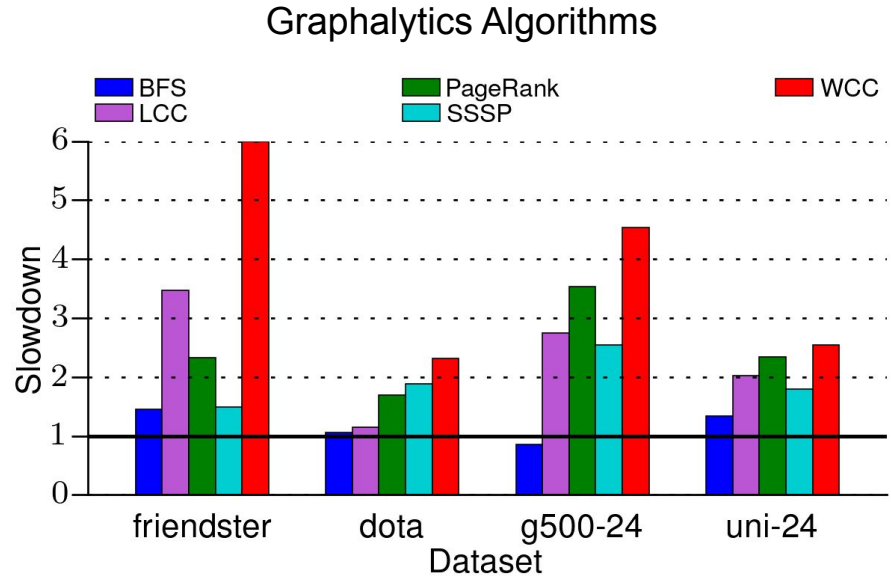
# Which Vertex ID Domain to Store for Random Algorithmic-Specific Access?

sparse domain: {0, 3, 1000, 1001, ...}

---

normalized against

dense domain: [0, 1, 2, 3, ...]



# Transactions in Graphs

Fall into two categories (mostly):

1. long-running, read-only transactions
  - a. between seconds and multiple minutes
  - b. e.g. PageRank (analytics), SSSP (traversals), triangle counting (GPM)
2. simple write-only transactions,
  - a. with a-priori known read- and write-sets
  - b. e.g. edge insertions

# Transactions on Graphs (cont.)

- versioned records are 8 Bytes or less
- requires low overhead per version
  - we expect mostly 1 or 2 versions for each record
- our overhead is 0 for single versions, 8 Bytes for 2 versions and 16 Byte per additional version

# Requirements for Concurrency Control

1. decouple reads from writes → use MVCC
2. high throughput for simple writes with known write-set → conservative two phase locking with fixed locking order



# Transactions

- Example: inserting the undirected edge  $(a, b)$  with  $b < a$ 
  1. Acquire locks for vertex  $b$  then  $a$
  2. Check if  $a$  and  $b$  exists, ensure neither  $(a, b)$  nor  $(b, a)$  exist
  3. Draw commit timestamp
  4. Insert  $(a, b)$  and  $(b, a)$
  5. Release locks

Avoids overheads of other protocols, e.g. drawing two timestamps, deadlock detection, and rollback handling.

# Real world graph workloads are diverse

Top 5 most common graph workloads according to a survey [VLDB, 2017]

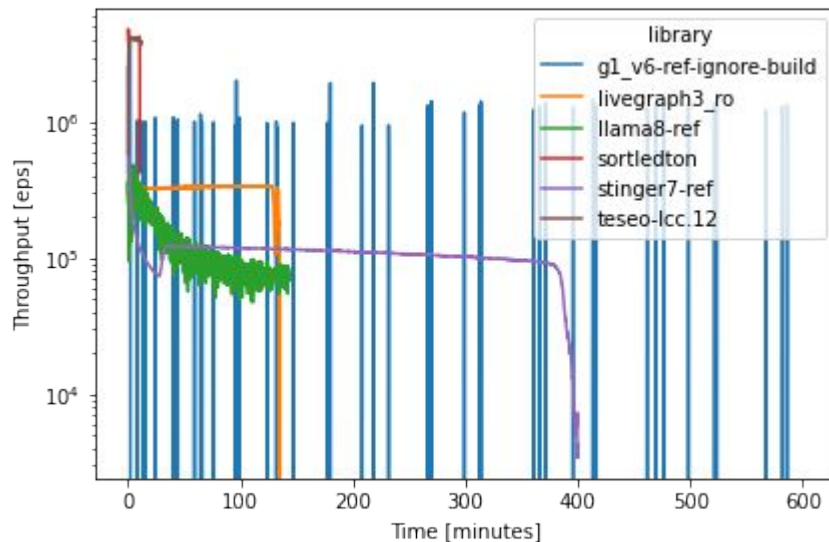
Workload categories [arxiv, 2019]

Computation	Total
Finding Connected Components	55
Neighborhood Queries (e.g., finding 2-degree neighbors of a vertex)	51
Finding Short / Shortest Paths	43
Subgraph Matching (e.g., finding all diamond patterns, SPARQL)	33
Ranking & Centrality Scores (e.g., PageRank, Betweenness Centrality)	32

- analytical
- neighborhood
- traversals
- graph pattern matching
  - used in analytical and transactional settings

# Aging throughput over time

- Teseo and Sortledton provide high, stable throughput
- Livegraph has low, stable throughput
- LLama throughput diminishes over time
- Graphone has severe issues with edge removals



# Properties of existing approaches

	<b>GraphOne</b>	<b>LLama</b>	<b>Stinger</b>	<b>Livegraph</b>	<b>Teseo</b>	<b>Us</b>
<b>Intersections</b>	No	No	No	No	Sorted	Sorted
<b>Sequential Scans</b>	blocks	blocks	blocks	vector	blocks	blocks
<b>Skewed insertions</b>	$O(D)$	N/A	$O(D)$	$O(D)$	$O(\log D)$	$O(\log D)$
<b>Vertex identifiers</b>	dense	user needs to provide dense vertices	dense (no deletions)	user needs to provide dense vertices	sparse	concurrent sparse to dense translation
<b>Edge Contiguous</b>	no	partially	no	no	yes	no